## 1.5 Convolutional Neural Networks

### 1.5.1 Basic ConvNets

• We use a filter to take a dot product with a portion of an image. So given some  $n^{[l-1]} \times n^{[l-1]}$  input, using a  $f \times f$  filter with padding p and stride s, our output is size

$$n^{[l]} = \frac{n^{[l-1]} - f + 2p}{s} + 1 .$$
(12)

We run many filters for each input image. Formally, given some input image of shape  $(n_h^{[l-1]}, n_w^{[l-1]}, n_c^{[l-1]})$ , we can use a filter of shape  $(f^{[l]}, f^{[l]}, n_c^{[l-1]})$  with padding  $p^{[l]}$  and stride  $s^{[l]}$  where the weights are shape  $(f^{[l]}, f^{[l]}, n_c^{[l-1]}, n_c^{[l]})$  and the bias is shape  $(1, 1, 1, n_c^{[l]})$  to produce an output of shape  $(n_h^{[l]}, n_w^{[l]}, n_c^{[l]})$ .

- Typically, max pooling (or average pooling) layers are also used, with f = 2 and s = 2.
- Three classic networks:
  - LeNet-5 (60k parameters): trained on MNIST with  $2 \times (\text{conv} + \text{pool})$  layers with two FC layers.
  - AlexNet (60M parameters): worked on ImageNet, similar to LeNet but had 8 layers.
    - \* Much deeper than LeNet-5, and stacked convolutional layers directly on top of each other without a max pooling layer in between.
    - $\ast\,$  Used the ReLU activation function.
    - \* Used local response normalization (normalize activations on the  $n_c$  axis, doesn't help much).
    - \* Used data augmentation and dropout to reduce overfitting. Multiple GPUs.
  - VGG-16 (138M parameters): simple because it used convolutions with  $3 \times 3$  filters with s = 1 and max pooling with f = 2 and s = 2.
- Filters for edge detection:

### 1.5.2 ResNet

- Context: deep networks are harder to train because of the exploding/vanishing gradient problem. In theory, training error should go down for deeper networks, but in practice, training error went up after some point for deeper networks.
- ResNet solved this problem by introducing skip connections. We have

$$a^{[l+2]} = g(z^{[l+2]} + a^{[l]}) . (13)$$

Because  $z^{[l+2]} = w^{[l+2]}a^{[l+1]} + b^{[l+2]}$ , when  $w^{[l+2]}$  and b[l+2] are 0, then  $a^{[l+2]} = a^{[l]}$ , so it's easy to learn the identity function.

#### 1.5.3 Inception Net

- 1×1 convolutions are very important. While for an input with only one channel, you're just multiplying by one number, for multiple channels, you're multiplying the number in each channel by some weight, summing it, and applying an activation function. You can think of it as a small FC layer.
- In an inception module, instead of picking the filter sizes, you can use  $1 \times 1$ ,  $3 \times 3$ , and  $5 \times 5$ , and maxpool layers, and stack their outputs together.

- The cost of computing some outputs, however, can be large. For instance, for an input of (28, 28, 192) with a 5 × 5 convolutional layer with same padding and 32 channels, you have to do  $28 \times 28 \times 32 \times 5 \times 5 \times 32 = 120M$  computations. You can reduce this by using a 1 × 1 convolution to decrease the number of channels in the input from size 192 to 16, for example.
- The main innovation is that inception modules allow for deeper nets with much fewer parameters.

# 1.5.4 Q & A

- Why do we use ConvNets?
  - Two reasons we use convolutions are (1) they share parameters and (2) the sparsity of connections (in each layer, each output value only depends on a small number of inputs).
  - For why ConvNets work better than DNNs on images, (A) kernels can detect features anywhere on the image, and features often repeat in images, and (B) ConvNets get the prior that nearby pixels are close, while DNNs do not know how pixels are organized.